

### Efficiency Problems—Additional Practice

Efficiency is the ratio of the useful energy output of a device to the energy input required to operate the device. To determine the efficiency and percent efficiency, we can use the following equations:

$$\text{eff} = \frac{E_{\text{out}}}{E_{\text{in}}} \text{ and } \% \text{ eff} = \frac{E_{\text{out}}}{E_{\text{in}}} \times 100\%$$

where  $\text{eff}$  is the efficiency,  $E_{\text{out}}$  is the useful energy output, and  $E_{\text{in}}$  is the energy input. We can also use power to determine the efficiency and percent efficiency of an energy-transforming device in the following equations:

$$\text{eff} = \frac{P_{\text{out}}}{P_{\text{in}}} \text{ and } \% \text{ eff} = \frac{P_{\text{out}}}{P_{\text{in}}} \times 100\%$$

where  $\text{eff}$  is the efficiency,  $P_{\text{out}}$  is the useful power output, and  $P_{\text{in}}$  is the power input. Solve each of the following problems in the space provided. Be sure to express your answers properly.

#### Sample Problem

A person exerts a power of 165 W in lifting a 10.0 kg object vertically a distance of 3.0 m in a time of 2.0 s. What is the percent efficiency of the lift?

$$P_{\text{in}} = 165 \text{ W}$$

$$m = 10.0 \text{ kg}$$

$$g = 9.8 \text{ N/kg}$$

$$h = 3.0 \text{ m}$$

$$E_{\text{out}} = E_g$$

$$E_g = ?$$

$$E_g = mgh$$

$$= (10.0 \text{ kg})(9.8 \text{ N/kg})(3.0 \text{ m})$$

$$= 294 \text{ J}$$

$$E_{\text{out}} = 294 \text{ J}$$

$$\Delta t = 2.0 \text{ s}$$

$$P_{\text{out}} = ?$$

$$P_{\text{out}} = \frac{E_{\text{out}}}{\Delta t}$$

$$= \frac{294 \text{ J}}{2.0 \text{ s}}$$

$$= 147 \text{ W}$$

$$\begin{aligned}\% \text{ eff} &= \frac{P_{\text{out}}}{P_{\text{in}}} \times 100\% \\ &= \frac{147 \text{ W}}{165 \text{ W}} \times 100\% \\ &= 89\%\end{aligned}$$

The percent efficiency of the lift is 89%.

1. A 1.2-kW electric kettle takes 5.0 min to bring one litre of water from 20°C to the boiling point. If it requires  $3.4 \times 10^5$  J of thermal energy to perform this task, what is the kettle's efficiency?
2. A car's engine is rated at 225 hp. If the engine is 25% efficient, how much work can it do in 6.0 s? (1 hp = 746 W)
3. A pulley system is 78% efficient. If the system raises a 42-kg object vertically a distance of 8.0 m, how much energy does the operator of the pulley use?
4. A solar panel is 12% efficient. How much light energy falls on the panel each minute if the panel supplies 2.8 W of power?
5. An electric winch exerts a force of  $2.3 \times 10^3$  N in pulling an  $8.0 \times 10^2$ -kg boat along a marine railway for 11 m. At the end of the ramp, the boat is 2.0 m above the water level. What is the efficiency of the ramp?